Effect of Heat Source on Mixed Convection of Non-Newtonian Fluids through Porous Medium along A Heated Vertical Flat Plate

P. K. Agarwal *, Yogendra Kumar Dwivedi

Department of Mathematics, Ganjdundwara College, Ganjdundwara, Kasganj, Uttar Pradesh, India

Article Info

Article history:

Received 30 September 2014 Received in revised form

20 October 2014

Accepted 20 November 2014 Available online 15 December 2014

Keywords

Mixed Convection, Boundary Layer, Non-Newtonian, Modified Power Low, Finite Difference, Flat Plate, Porous Medium, Heat Source

Abstract

The present paper is to study of an effect of heat source on mixed convective heat transfer of non-Newtonian fluids through porous medium on a flat plate has been investigated using a modified power – law viscosity model. This model does not contain physically unrealistic limits of zero or infinite viscosity as are encountered in the boundary - layer formulation with traditional models of viscosity for power – law fluids through porous medium with magnetic field. These unrealistic limits can introduce an irremovable singularity at the leading edge; The present modified model matches well with the measurement of viscosity, and does not introduce irremovable singularities. Therefore, the boundary layer equations can be solved by marching from the leading edge downstream as for Newtonian fluids. The numerical results are presented for a shear-thinning fluid in terms of the velocity and temperature distribution, and for important physical properties, namely the wall shear stress and heat transfer rates.

Nomenclature

C constant

C_f dimensionless shear stress coefficient D non-dimensional viscosity of the fluid

Grashof number

g acceleration due to gravity
 k dimensional constant
 K porosity parameter

reference length scale of the plate non-Newtonian power-law index

Nu Nusselt numberRe Reynolds numberS heat source parameter

($\overline{\mathcal{U}}$, $\overline{\mathcal{V}}$) Fluid velocities in the ($\overline{\mathcal{X}}$, $\overline{\mathcal{Y}}$)directions,

respectively.

(U, V) dimensionless fluid velocities in the (ξ, η) directions, respectively.

 U_0 free-stream velocity

T dimensional temperature of the fluid

 T_w surface temperature T_∞ ambient temperature

Greek symbols

 ξ axial direction along the plate pseudo-similarity variable

 γ shear-rate ρ fluid density

v viscosity of the non-Newtonian fluid v₁ reference viscosity of the fluid

α thermal diffusivity

 θ dimensionless temperature of the fluid

1. Introduction

Free convection can have significant effects on forced flows over solid bodies. It can alter the flow field and, hence

Corresponding Author,

E-mail address: pk.ganj@gmail.com All rights reserved: http://www.ijari.org the heat transfer rate and the wall shear stress. Such effects are particularly enhanced for high-speed rotating machineries due to their large centrifugal forces. The effect of natural convection is accumulative so it cannot be ignored even when the flow acceleration is small. The simplest physical model is a two-dimensional mixed forced and free convection along a flat plate. Understanding of fundamental mechanism of this interaction can help to estimate more accurately the heat transfer rate and pumping power for complex geometries of practical interest in order to prevent unnecessary burn-out of heated surfaces.

The interest in heat transfer problems involving powerlaw, a non-Newtonian fluid has grown persistently in the past half century. An excellent sequence of lectures on non-Newtonian fluids was given by Hinch [1]. It appears that Acrivos [2], a frequently cited paper, was the first to consider boundary – layer flows for such fluids. Since then, a large number of related papers have been published due to their wide relevance in chemicals, foods, polymers, molten plastics and petroleum production, and other natural phenomena. A complete literature survey would be impractical; a few references, which can be used as starting points for a more extensive search [3-13], are listed here.

Two widespread mistakes appear continuously in papers studying boundary-layers involving the traditional two-parameter power-law model of non-Newtonian fluids (see Bird et al. [14]).

The first is that few authors recognize that length scale is associated with the power-law correlation. Due to this length scale, boundary layer problems with power – law, non-Newtonian fluids cannot have simple self-similar solutions. It is nevertheless a common practice to ignore, without justification, the dependence of boundary – layer solutions on the steam wise coordinate. It has been demonstrated in [15] that such a self –similar solution is actually only valid at the leading edge of the boundary-layer. This similarity solution is the required upstream

condition at the leading edge of the flat plate to integrate boundary-layer equations along the stream wise direction.

The second concern is related to the unrealistic physical results, introduced by the traditional power-law correlation, that viscosity either vanishes or becomes infinite in the limit of large or small shear rates, respectively. This usually occurs at the leading edge of a flat plate, or along the outer edge of boundary – layers where the boundary – layer matches with the outer inviscid flow. Thus, traditional power-law correlations introduce nonremovable singularities into boundary-layer formulations for infinite or zero viscosity. Without recognizing the cause of such unrealistic conditions, complex multi-layer structures have been introduced by many authors, for example, Denier et al. [12-13], to overcome certain mathematical difficulties in order to obtain solutions of a non-physical formulation, or a false starting process has been used to integrate boundary-layer equations from slightly downstream of the leading edge in order to avoid the irremovable singularity there [8-9].

A recently proposed modified power-law correlation is sketched for a number of values of the power index 'n'. It is clear that this new correlation does not contain physically unrealistic limits of zero and infinite viscosities as do traditional power-law correlations. The modified powerlaw, in fact, fits measured viscosity data better. The constants in the proposed model are fixed with available measurements and described in detail in [15], where the boundary-layer formulation on a flat plate is described and numerically solved. The associated heat transfer for two different heating conditions is reported [16]. A shearthinning fluid, whose power-law index is 0.95, slightly different from Newtonian fluids for which n = 1, was selected in the study of [15-16]. In [17-19], this analysis is extended to fluids whose power-law indexes are 0.6, 0.8, 1, 1.2 and 1.4 in order to fully demonstrate the effect of non-Newtonian fluids. In this paper, results for mixed convection of non-Newtonian fluids along a vertical flat plate using the modified power-law model for shear thinning fluid are presented. A similar analysis for natural convection along a vertical heated flat plate appears in [20]. Recently, Molla and Yao [22] have studied on mixed convection of non-Newtonian fluids along a heated vertical flat plate, It is known [21] that length scale exists for mixed convection boundary-layers for Newtonian fluids due to the interaction of the forced and the free convections; hence, there is no similarity solution for mixed convection boundary-layers. On the other hand, the Nusselt number and shear stress distributions can be well correlated in terms of this length scale for all combination of the Reynolds and Rayleigh numbers since the flows are laminar. This is not true for non-Newtonian fluids, since the new length scale, introduced into the formulation by the traditional power-law correlation, becomes the dominant length scale of mixed convection boundary-layers for power-law fluids through porous medium with magnetic field and heat source. This will be demonstrated by numerical results presented in

Formulation of Problem

A steady laminar boundary-layer of a non-Newtonian fluid through porous medium with magnetic field along a semi-infinite heated flat plate with heat source has been

studies. The viscosity depends on the shear rate and is correlated by a modified power-law for shear-thinning non-Newtonian fluids. It is assumed that the surface temperature of the plate Tw, where $T_w > T_{\infty}$ Here $T\infty$ ambient temperature of the fluid and T is the temperature of the fluid. The coordinate system is shown in Fig. 1.

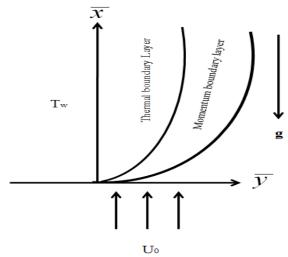


Fig: 1. Physical Model and Coordinates The equations governing the flow and heat transfer are

$$\frac{\partial \overline{u}}{\partial \overline{x}} + \frac{\partial \overline{v}}{\partial \overline{y}} = \mathbf{O} \qquad \dots (1)$$

$$\overline{u} \frac{\partial \overline{u}}{\partial \overline{x}} + \overline{v} \frac{\partial \overline{u}}{\partial \overline{v}} = \frac{\partial}{\partial \overline{v}} \left(v \frac{\partial \overline{u}}{\partial \overline{v}} \right) + g \beta \left(T - T_{\infty} \right) - \frac{v}{K} \overline{u} \dots (2)$$

$$\overline{u}\frac{\partial x}{\partial \overline{x}} + \overline{v}\frac{\partial x}{\partial \overline{y}} = \frac{\partial}{\partial \overline{y}} \left(v\frac{\partial x}{\partial \overline{y}}\right) + g\beta(T - T_{\infty}) - \frac{\partial}{\partial \overline{x}} \overline{u} \dots (2)$$

$$\overline{u}\frac{\partial T}{\partial \overline{x}} + \overline{v}\frac{\partial T}{\partial \overline{y}} = \alpha \frac{\partial^2 T}{\partial \overline{y}^2} + \overline{S}\left(T - T_{\infty}\right) \qquad \dots (3)$$

Where \overline{u} , \overline{v} are velocity components along the $(\overline{X}, \overline{Y})$ axes, T is the temperature, S is the heat source parameter and α is the thermal diffusivity of the fluid. The viscosity is correlated by a modified power-law, which is

$$v = \frac{k}{\rho} \left| \frac{\partial \overline{u}}{\partial \overline{y}} \right|^{n-1} \text{ for } \overline{\gamma}_1 \le \left| \frac{\partial \overline{u}}{\partial \overline{y}} \right| \le \overline{\gamma}_2 \qquad \dots (4)$$

The constant $\overline{\gamma}_1$, and $\overline{\gamma}_2$, are threshold shear rates, ρ is the density of the fluid, and k is a dimensional constant, whose dimension depends on the power – law index n. the values of these constants can be determined by matching with measurements. Outside of the above range, viscosity is assumed constant; its value can be fixed with data given in.

The boundary conditions for the present problem

$$\overline{u} = \overline{v} = 0, \quad T = T_{w} \quad at \quad \overline{y} = 0$$

$$\overline{u} = U_{0}, \quad T \to T_{\infty} \quad as \quad \overline{y} \to \infty$$

$$... (5)$$

Where U_0 is the free steam velocity

We now introduce the following non - dimensional

We now introduce the following non – dimensional transformulations
$$x = \frac{\overline{x}}{l}, \quad y = \frac{\overline{y}}{l} \operatorname{Re}^{1/2}, \quad u = \frac{\overline{u}}{U_0}, \quad v = \frac{\overline{v}}{U_0} \operatorname{Re}^{1/2}$$

$$K_0 = \frac{KU_0}{vl}, \quad \theta = \frac{T - T_{\infty}}{T_W - T_{\infty}}, \quad D = \frac{v}{v_1}, \quad S = \frac{\overline{S}l}{U_0}$$

$$\operatorname{Re} = \frac{U_0 l}{v_1}, \quad Gr = \frac{g \beta \Delta T l^3}{v_1^2}, \quad \operatorname{Pr} = \frac{v_1 \rho C p}{k} = \frac{v_1}{\alpha}$$

Where v_1 is the reference viscosity, θ is the dimensionless temperature of the fluid, Re is the Reynolds number and Gr is the Grashof number. The length scale is

$$l = C^{\frac{2}{1-n}} \left[\left(\frac{k}{\rho} \right)^2 \frac{1}{\nu_1^{n+1}} \right]^{\frac{1}{n-1}} U_0^3 \qquad \dots (6b)$$

Substituting variables (6a) into Eqs. (1) - (4) leads to the following non-dimensional equations

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0, \qquad \dots (7)$$

$$u\frac{\partial u}{\partial x} + v\frac{\partial u}{\partial y} = \frac{\partial}{\partial y} \left[D\frac{\partial u}{\partial y} \right] + \frac{Gr}{Re^2} \theta - Qu \qquad \dots (8)$$

$$\frac{\partial \theta}{\partial x} + v \frac{\partial \theta}{\partial y} = \frac{1}{\text{Pr}} \frac{\partial^2 \theta}{\partial y^2} + S\theta \qquad \dots (9)$$

$$D = \frac{k}{\rho v_1} \left(\frac{U_o}{l} \right)^{n-1} \left| \frac{\partial u}{\partial y} \right|^{n-1} = C \left| \frac{\partial u}{\partial y} \right|^{n-1} \qquad \dots (10)$$
Where

Where Pr is the Prandtl number. The physical meaning
$$Gr$$
 1 presents the ratio of the length

 $\frac{Gr}{\text{Re}^2} = \frac{1}{U^2/(\beta \Delta T)}$ presents the ratio of the length

scale that the non-Newtonian effect becomes apparent and the length scale that the natural convection effect grows

dominant. For larger $\frac{Gr}{Re^2}$, it takes shorter distance for

the effect of natural convection becomes dominant.

The boundary conditions (5) become

$$u = v = 0, \quad \theta = 1 \quad at \quad y = 0$$

$$u \to 1, \quad \theta \to 0 \quad as \quad y \to \infty$$
... (11)

Next the equations are transformed to parabolic

$$\xi = x$$
, $\eta = \frac{\hat{y}}{(2x)^{1/2}}$, $U = u$, $V = (2x)^{1/2}v$, $\theta = \theta(\xi, \eta)$

In order to remove the singularity at the leading edge, and to minimize the variation of the boundary-layer thickness for computational convenience. Consequently, Eqs. (7) - (9) become

$$(2\xi)\frac{\partial U}{\partial \xi} - \eta \frac{\partial U}{\partial \eta} + \frac{\partial V}{\partial \eta} = 0, \qquad \dots (13)$$

$$(2\xi)U\frac{\partial U}{\partial \xi} + (V - \eta U)\frac{\partial U}{\partial \eta} = \frac{\partial}{\partial \eta} \left[D\frac{\partial U}{\partial \eta} \right] + 2\xi \left(\frac{Gr}{Re^2}\theta - QU \right)$$

$$\dots (14)$$

$$(2\xi)U\frac{\partial \theta}{\partial \xi} + (V - \eta U)\frac{\partial \theta}{\partial \eta} = \frac{1}{\Pr} \frac{\partial^2 \theta}{\partial \eta^2} + S\theta$$

$$\dots (15)$$

$$\mathbf{D} = \begin{cases} & 1, & |\gamma| \leq \gamma_1 \\ & \left| \frac{\gamma}{\gamma_1} \right|^{n-1}, & \gamma_1 \leq |\gamma| \leq \gamma_2, & where & \gamma = \left(2\xi \right)^{-1/2} \frac{\partial U}{\partial \eta} \\ & \left| \frac{\gamma_2}{\gamma_1} \right|^{n-1}, & |\gamma| \geq \gamma_2 \end{cases}$$

The correlation (16) is a modified power-law correlation first presented by Yao and Molla [15], This correlation describes that if the shear rate $|\gamma|$ lies between the threshold shear rates y_1 and y_2 then the non-Newtonian viscosity, D, varies with the power-law of γ . On the other hand, if the shear rate $|\gamma|$ do not lie within this range, then the non-Newtonian viscosities are different constants as shown in. This is property of many measured viscosities.

Eqs. (13) - (15) can be solved by marching downstream with the upstream condition satisfying the following differential equations.

$$-\eta \frac{\partial U}{\partial \eta} + \frac{\partial V}{\partial \eta} = 0, \qquad \dots (17)$$

$$(V - \eta U) \frac{\partial U}{\partial \eta} = \frac{\partial}{\partial \eta} \left[D \frac{\partial U}{\partial \eta} \right] \qquad \dots (18)$$

$$(V - \eta U)\frac{\partial \theta}{\partial \eta} = \frac{1}{\text{Pr}} \frac{\partial^2 \theta}{\partial \eta^2} + S\theta \qquad \dots (19)$$

Which are the limits of Eqs. (17) - (19) as $\xi \to 0$. The corresponding boundary conditions are

$$U = V = 0, \quad \theta = 1 \text{ at } \quad \eta = 0$$

$$U \to 1, \quad \theta \to 0 \quad \text{as} \quad \eta \to \infty$$

$$... (20)$$

Eqs. (13) - (15) and (17) - (19) are discredited by a central - difference scheme for the diffusion term and a backward-difference a scheme for the convection terms; finally we get a system of implicit tridiagonal algebraic system of equations. The algebraic equations have been solved by a double - sweep technique. In the computation the continuity equation is directly solved for the normal velocity component V. hence, the truncation errors are

 $O\left(\Delta\xi\right)$. The computation is started from $\xi=0.0$ and then marches downstream to $\xi=100$. After several test runs, convergent results are obtained by using $\Delta\xi=2\times10^{-9}$ and $\Delta\eta=0.1$ near the leading edge from $\xi=0.0$ to $\xi=10^{-6}$ afterwards $\Delta\xi$ is gradually increased by the relation $\Delta\xi^{(new)}=2\Delta\xi^{(old)}$ up to $\Delta\xi=0.005$

The physical quantities of principle interest are the wall shear stress in terms of the skin – friction coefficient C_f and the rate of the heat transfer in terms of the Nusselt number Nu, which are, respectively,

$$C_{f} \left(2\xi \right)^{1/2} = \left[D \frac{\partial U}{\partial \eta} \right]_{r=0} \tag{21}$$

$$Nu\left(2\xi\right)^{-1/2} = -\left(\frac{\partial\theta}{\partial\eta}\right)_{\eta=0} \tag{22}$$

3. Results and discussion

Numerical results are presented for the case of a non-Newtonian power-law fluid of shear – thinning (n=0.6) case along with Newtonian fluid (n=1.0) for the value of the Prandtl number Pr=1.2. Computations have been done for threshold shear rates limits of $\gamma_1=0.1$ and $\gamma_2=10^5$ and for two values of the mixed convection parameter Gr/Re^2 (= 0.1 or 1.0). The non-dimensional viscosity, D, given by the modified power-law correlation, which is plotted in as a function of the non-dimensional shear rate γ . The singularity experienced at the leading edge for the traditional power-law correlation has been successfully removed without any difficulty by using the present modified power-law correlation. Since the shear stress at the leading edge is

inversely proportional to $\sqrt{2\xi}$ it is infinite there, and D

$$= \left(\frac{\gamma_2}{\gamma_1}\right)^{n-1}$$
 at the leading edge.

The velocity distribution as a function of η at selected ξ locations for the power law index n=0.6 are depicted in Figures – (1) and (2) for $Gr/Re^2=0.1$ and $Gr/Re^2=1.0$, respectively at $\xi=0$, the velocity distribution is the forced convection similarity velocity profile, from figures – (1) and (2), it is observed that the natural convection has a significant influence on the flow field. For $Gr/Re^2=0.1$, it takes longer distance for the natural convection effect becomes dominant. On the other hand, for $Gr/Re^2=1.0$, the natural convection takes short distance becomes the dominant mode. The velocity distribution is the natural convection has a significant influence on the flow field for porosity. The velocity distribution increases due to increase the value of porosity parameter (K) in figure – (3).

The corresponding temperature distributions are plotted Figures - (4), (5) and (6), respectively, for different values of ξ , Pr and S at $Gr/Re^2 = 0.1$, the temperature distribution is larger than any other location since, near $\xi = 1$, In figure – (4), the temperature distribution is enhanced due the

combined mode of forced and natural convection. On the other hand, the temperature distribution decreases as increase in the case of ξ , which is expected due to the natural convection mode. In figure - (5), the temperature distribution decreases due to increase the values of Pr for natural convection. In figure - (6), the temperature distribution increases due to increase the values of heat source parameter S for the combined mode of forced and natural convection.

The axial distribution of the skin - friction coefficient

$$C_{_f}(2\xi)^{^{1\!\!/2}}$$
 and the Nusselt number $Nu(2\xi)^{^{-1\!\!/2}}$ are

derived in equations – (21) and (22), respectively, for Pr = 1.2, n = 0.6 and $Gr/Re^2 = 0.1$, with the forced convection limit. It is observed that the forced convection solutions coincide with the full mixed convection solutions for comparison, we have provided only forced convection solutions because the forced convection and the mixed convection length scales are same for the non-Newtonian fluids, but it is difficult to compare with the mixed and free convection solutions due to the different length scales [20]. They clearly show that the free convection effects grow faster for larger Gr/Re^2 . The data for the Newtonian fluids (n = 1) with shear-thinning non-Newtonian fluid (n = 0.6) to contrast the differences of the two fluids. From this comparison it is observed that the skin-friction coefficient decreases and the Nusselt number increases for the shear –

thinning fluid. Which can correlate $C_{\scriptscriptstyle f}(2\xi)^{1\!\!/2}$ and

 $Nu(2\xi)^{-1/2}$ into a single curve for all combination of Gr and Re for Newtonian fluids [21]. But not for non-Newtonian fluids. This indicates that the length scale introduced by the interaction of forced and free convections is not the proper length scale for non-Newtonian fluids. Consequently, we use the length scale associated with the power-law in the current study.

4. Conclusions

The proposed modified power-law correlation fits well with the actual measurement of viscosities for non-Newtonian fluids; consequently it does not contain physically unrealistic limits of zero and infinite viscosity introduced into the boundary - layer formulation by the traditional power-law model. The problems associated with the non-removal singularity introduced by the traditional power-law correlations do not exist for the modified powerlaw correlation proposed in this paper. This means that the similarity solution exists at the leading edge, which is the natural upstream condition for the non-similar boundary layer problem. Therefore, the proposed modified power-law correlations can be used to investigate other heat transfer problems for shear - thinning or shear thickening non-Newtonian fluids on boundary - layers. The fundamental mechanism that the effect of natural convection eventually becomes dominant when the heating length is long is also properly demonstrated in our computations. For the low heating case with $Gr/Re^2 = 0.1$, the effect of natural convection has not reached its fully developed stage at =100.

References

- J. Hinch, Non-Newtonian geophysical fluid dynamics, Program in geophysical fluid dynamics, woods hole oceangraphic institution woods, Hole, MA 02543 USA, 2003. Available from:
- [2] A, Acrivos, A theoretical analysis of laminar natural convection heat transfer to non-Newtonian fluids, AIChE J. 16, 1960, 584-590.
- [3] F. Emery, H.S. Chi, J. D Dale, Free convection through vertical plane layers of non-Newtonian power-law fluids, ASME J. Heat transfer, 93,1970, 164-171.
- [4] T. V. W. Chen, D.E. Wollersheim, Free convection at a vertical plate with uniform flux conditions in non-Newtonian power-law fluids. ASME J. Heat transfer. 95, 1973 123-124.
- [5] Z. P. Shulman, V.I. Baikov, E.A. Zaltsgendler, An approach to prediction of free convection in non-Newtonian fluids, Int. J. Heat mass transfer, 19, 1976, 1003-1007
- [6] A. Som, J. L. S. Chen, Free convection of non-Newtonian fluids over non-isothermal two-dimensional bodies, Int. J. Heat Mass transfer, 27, 1984, 791-794
- [7] S. Haq. C. Kleinstreuer, J. C. Mulligan, Transient free convection of a non-Newtonian fluid along a vertical wall, ASME J. heat transfer, 110, 1988, 604-607
- [8] M. J. Huang, J. S. Huang, Y. L. Chou, C.K. Cheng, Effects of Prandtl number on free convection heat from a vertical plate to a non-Newtonian fluid, ASME J. Heat transfer 111, 1989, 189-191
- [9] M. J. Huang, C. K. Chen, Local similarity solutions of free –convective heat transfer from a vertical plate to non-Newtonian power-layer fluids. Int. J. Heat mass transfer, 33, 1990, 119-125
- [10] E. Kim. Natural convection along a wavy vertical plate to non-newtonian fluids. Int. J. Heat mass transfer. 40, 1997, 3069-3078
- [11] W. A. Khan, J. R. Culham, M. M. Yovanovich, Fluid flow and heat transfer in power-law fluids across circular cylinders: analytical study. J. Heat transfer. 128, 2006, 870-878
- [12] J. P. Denier, P. P. Dabrowski, On the boundary layer equations for power-law fluids, Proc. R. Soc. Lond. A 460(2051), 2004, 3143-3158
- [13] J. P. Denier. R. E. Hewitt, Asymptotic matching constraints for a boundary – layer flow of a power – law fluid. J. Fluid Mech 518, 2004, 261-279
- [14] R. B. Bird, R. C. Armstrong, O. Hassager, Dynamics of polymer liquids, 1, Fluid Mech. 2nd ed. Wiley, New York, 1987
- [15] L. S. Yao, M. M. Molla, Flow of a non-Newtonian fluids on a flat plate: I boundary layer. J. Thermophys. Heat transfer, 22(4), 2008, 758-761
- [16] M. M. Molla, L. S. Yao, Flow of a non –Newtonian fluids on a flat plate: II Heat transfer, J. Thermophys. Heat transfer 22(4), 2008, 762-765
- [17] M. M. Molla, L. S. Yao, Flow of a non –Newtonian fluids on a flat plate a uniform heat flux, ASME, J. Heat transfer. 131, 2009, 1-6
- [18] L. S. Yao, M. M. Molla, forced convection of non-Newtonian fluids on a heated flat plate, Int. J. Heat mass transfer, 51, 2008, 5154-5159

- [19] M. M. Molla, L. S. Yao, Natural convection non-Newtonian fluids along a vertical plate plate with a uniform heat flux, J. Thermophys. Heat transfer, 2008
- [20] S. G. Moulic, L. S. Yao, Non-Newtonian natural convection along a vertical flat plate with uniform surface temperature. J. Heat transfer, 2008
- [21] L. S. Yao, Two dimensional mixed convection along a flat plate, ASME J. Heat transfer, 109, 1987, 440-445
- [22] M. M. Molla, L. S. Yao, Mixed convection of non-Newtonian fluids along a heated vertical flat plate, Int. J. heat and mass transfer, 52, 2009, 3266-3271

IJARI 799